

Solution ① (a) (i)

As quadratic eqⁿ given,

$$8x^2 - x - 2 = 0 \quad \text{--- ①}$$

Discriminant, $D = b^2 - 4ac$.

$\left\{ \begin{array}{l} \because b \rightarrow \text{coefficient of } x \\ a \rightarrow \text{coefficient of } x^2 \\ c \rightarrow \text{constant.} \end{array} \right.$

$$\therefore b = (-1)$$

$$a = 8$$

$$c = (-2)$$

$$\therefore D = b^2 - 4ac$$

$$= (-1)^2 - 4(8)(-2)$$

$$= 1 + 64$$

$$[D = 65]$$

Solution ① (a) (ii)

$$D = b^2 - 4ac$$

General quadratic eqⁿ
($ax^2 + bx + c = 0$)

(i) $D > 0 \rightarrow$ 2 Real and distinct solution.

as $D = 65 > 0 \rightarrow$ 2 Real & distinct solⁿ.

Solution ① (a) (iii)

As $D > 0$ & $a > 0$

So, graph will be upward parabola cutting x-axis at two different points
(α, β) \rightarrow roots of quadratic eqⁿ.

Solution ① (b)

$$y = -x^2 + 2x + 35$$

The axis of symmetry is a vertical line

$$x = \frac{-b}{2a}$$

$\left\{ \begin{array}{l} \because b \rightarrow \text{coeff. of } x \\ a \rightarrow \text{coeff. of } x^2 \end{array} \right.$

$$\therefore x = \frac{-2}{2(-1)} = 1 \quad \checkmark$$

Solution (i) / (b) / (ii)

→ calculating $x = 1$ put in standard eqⁿ.

$$\begin{aligned}y &= -x^2 + 2x + 35 \\&= -1^2 + 2 \cdot (1) + 35 \\&= -1 + 2 + 35 \\y &= 36\end{aligned}$$

∴ Coordinates of vertex (1, 36).

Solution 1/2(i)

$$x^2 - 14x + 11 = 0.$$

By completing square Method,

$$x^2 - 2 \cdot 7 \cdot x + (7)^2 - (7)^2 + 11 = 0$$

$$x^2 - 2 \cdot 7 \cdot x + (7)^2 - 38 = 0$$

$$(x-7)^2 - 38 = 0 \rightarrow \underline{\text{Ans}}$$

Solution 1/2(ii)

from above solⁿ in 1/2(i)

$$(x-7)^2 = 38$$

$$x-7 = \pm\sqrt{38}$$

$$x-7 = +\sqrt{38}$$

$$x = 7 + \sqrt{38}$$

$$x-7 = -\sqrt{38}$$

$$x = 7 - \sqrt{38}$$

Solution (i) / (ii) / (iii)

Vertex of quad. eqn .

$$y = x^2 - 14x + 11 \quad \text{--- (1)}$$

x-intercept

$$x = (13.16, 0) \text{ \& } (0.8, 0)$$

$$\text{Eqn of axis} = \frac{-b}{2a}$$

$$= -\frac{(-14)}{2(1)}$$

$$x = 7$$

\therefore put in $(x=7)$ in (1)

$$(y = -38)$$

\therefore vertex is $(7, -38)$ //

Solution (i) (ii) (iv)

\therefore x-intercepts $(13.16, 0)$ & $(0.84, 0)$

y-intercept - $(0, 11)$

equation of axis =

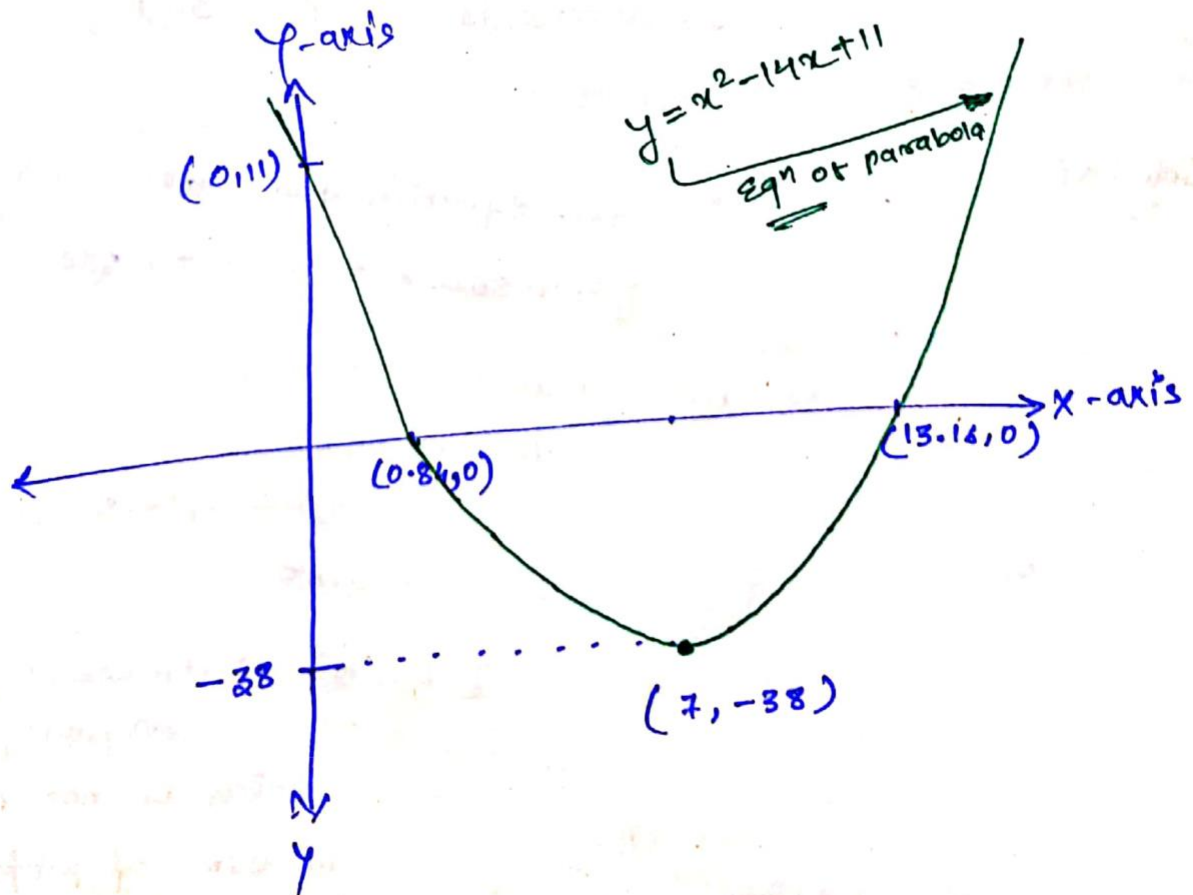
$$x = \frac{-b}{2a}$$

$$[x = 7]$$

\therefore vertex of parabola.

$$(7, -38)$$

$$\left(\because x=7 \text{ in } y = x^2 - 14x + 11 \right. \\ \left. y = -38 \right)$$



Solution (a) / (b)

Considering the equation that Aikta evaluates.

$$y = 4.862x^2 - 7.211x + 4.836.$$

as discriminant -

$$D = b^2 - 4ac$$

$$= (-7.211)^2 - 4(4.862)(4.836)$$

$$= -42.05$$

[$D < 0$] \rightarrow Hence, it produce
imaginary roots
which is not possible
in terms of profit.

Solution 2/6

$$y = -7.291x^2 + 5.771x - 0.502 \quad \text{--- (1)}$$

(i) on calculating y-intercept

$$(x=0)$$

put in eqⁿ (1)

$$y = -0.502$$

Solution 2/6 (ii)

'y' would be "Negative" because if No smoothie will be made ($x=0$) then Raw Material would get wasted leads to loss.

Solution 2/6 (iii)

$$y = -7.291x^2 + 5.771x - 0.502 \quad \text{--- (1)}$$

put ($y=0$) in eq (1)

$$0 = -7.291x^2 + 5.771x - 0.502$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$\left\{ \begin{array}{l} \because b = 5.771 \\ a = -7.291 \\ c = -0.502 \end{array} \right.$$

$$= \frac{-5.771 \pm \sqrt{(5.771)^2 - 4(-7.291)(-0.502)}}{2(-7.291)}$$

$$x_1 = 0.099 \quad | \quad x_2 = 0.692$$

Solution (2) (b) (iv)

As on calculating x -intercept on previous question.

$$x_1 = 0.099 \quad | \quad x_2 = 0.692$$

Hence minimum amount of smoothie that company need to produce is

$$x = 0.099 \text{ thousand ltr.}$$

Solution (2) (b) (v)

$$y = -7.291x^2 + 5.771x - 0.502 \quad \text{--- (1)}$$

$$x = 0.5 \text{ (given in ques.)}$$

put in (1)

$$y = -1.822 + 2.885 - 0.502$$

$$\{ y = 0.5615 \}$$

Hence target profit will not be achieved, by Aikta's equation.

Question 3 (Answer)

Soln. 3(a)

Dot plot → A frequency plot that shows the number of times a response occurred in a data set, where each data value is represented a dot.

We don't think it's a good idea because in this particular question we have total 40 data points.

20 of each (2019 & 2020 - year)

which make it very confusing, and hard to interpret what exactly data is showing, rather it becomes ~~over-crowded~~ over-crowded.

Solution 3(b) :- (Reference to subsection 1.2 of unit 11 is ^{Not} provided.)

But our views to improve the clarity of representation of Boxplots :-

1) Both plots should be firstly assigned for particular year - (data representation)

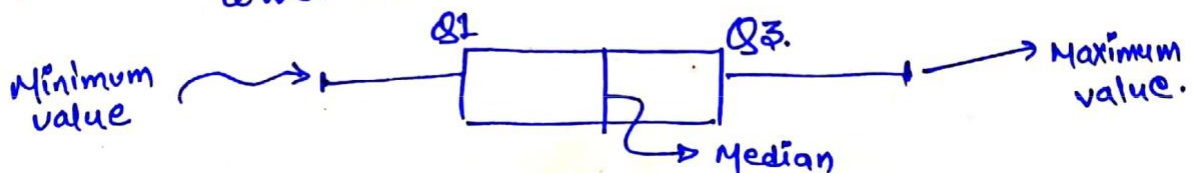
2) Exact values should be retained. i.e., in between two intervals values should be mentioned.

Solution 3(c) :- for reference check raw data as minimum value for

'2020' year → 0

'2019' year → 8

So, upper box plot is of 2020 year employee data.
lower box plot is of 2019 year " " .



Solution 3(d) (i) False,

Employees worked more hours in 2019

as Average working hours = ~~32.4 hours~~ 33.7 hours.

← Average working hours of 2020 = 31.05 hours.

Soln 3(d) (ii) (TRUE,)

Explanation:- variability in Box plot is measured by (IQR)

$$\begin{aligned} \text{IQR} &= Q_3 - Q_1 \\ &\leftarrow \text{(Interquartile Range)} \end{aligned}$$

IQR - for (2019) year

$$\begin{aligned} Q_3 &= 40 \\ Q_1 &= 25 \end{aligned} \quad \left. \vphantom{\begin{aligned} Q_3 &= 40 \\ Q_1 &= 25 \end{aligned}} \right\} \begin{aligned} \text{IQR} &= Q_3 - Q_1 \\ &= 40 - 25 \\ &= 15 \end{aligned}$$

IQR for (2020) - year

$$\begin{aligned} Q_3 &= 41.5 \\ Q_1 &= 22 \end{aligned} \quad \left. \vphantom{\begin{aligned} Q_3 &= 41.5 \\ Q_1 &= 22 \end{aligned}} \right\} \begin{aligned} \text{IQR} &= Q_3 - Q_1 \\ &= 41.5 - 22 \\ &\Rightarrow 19.5 \end{aligned}$$

$$\therefore \text{IQR}|_{2020} > \text{IQR}|_{2019} \quad \checkmark$$

Solution 3 (d) → (iii) (FALSE)

Explanation:-

Employee working hours . Data.

0
0
8
16
20
24
28
32
35
35 →
36
37
38
40
41
42
45
47
48
49

$$\text{Median} = \frac{35+36}{2} = 35.5$$

Explanation:-

Only half of the employees worked more than the Median values of hours.

Solution 3 (e) :- As on observing the box and whisker data are skewed on left i.e., negatively skewed.

Reason:- When the median is closer to the top of the box, and if the ~~upper~~ whisker is shorter on the upper end of the box, then the distribution is negatively skewed.

eg:-



Solution 3 (f) - (i)

figure 4 - belongs to 2020 year employee Data.
figure 3 - belongs to 2019 " " "

Reason :- Because in 2019 year's data, there is
no employee working hours lies between
30 - 35 range.

while in 2020 years - employees data lies between
30 - 35 range of working hours.

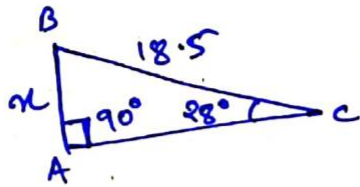
Solution 3 (f) - (ii)

Histogram provide us more insightful look at
frequency distribution as compared to
the Boxplot representation.

Solution 3 (f) - (iii) Box-plot allows us to compare given various
data set better than histogram. as Boxplots
summarizes variation in data set visually.

Solution 4:-

(a)



In given $\triangle ABC$,
apply sin law,

$$\frac{18.5}{\sin 90^\circ} = \frac{x}{\sin 28^\circ}$$

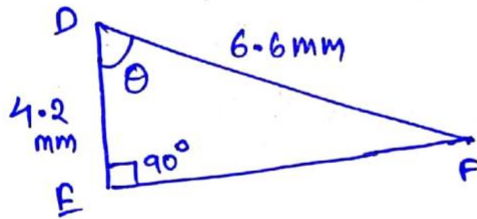
On cross multiplication,

$$\Rightarrow x = \sin 28^\circ \times \frac{18.5}{\sin 90^\circ}$$

$$= 0.4694 \times 18.5$$

$$[x = 8.6 \text{ cm}] \checkmark$$

Solution 4 (b)



Apply Pythagoras theorem,

$$(DF)^2 = (DE)^2 + (EF)^2$$

$$(6.6)^2 = (4.2)^2 + (EF)^2$$

$$EF = \sqrt{(6.6)^2 - (4.2)^2}$$

$$[EF = 5.09]$$

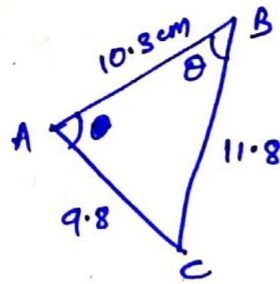
As we know,

$$\sin \theta = \frac{5.09}{6.6} = 0.77$$

$$\theta = \sin^{-1}(0.771)$$

$$= 50.47^\circ$$

Solution 4 (c) - (i)



Applying cosine law,

$$c^2 = a^2 + b^2 - 2ab \cos \theta$$

$$\text{let } c = 9.8 \text{ cm}$$

$$a = 10.3 \text{ cm}$$

$$b = 11.8 \text{ cm}$$

$$\therefore (9.8)^2 = (10.3)^2 + (11.8)^2 - 2(10.3)(11.8) \cos \theta$$

$$96.04 = 245.53 - 243.08 \cos \theta$$

$$\cos \theta = 0.6141$$

$$\theta = \cos^{-1}(0.6141)$$

$$[\theta = 52.11^\circ]$$

Soln 4 (c) - (ii)

$$\text{Area of } \triangle ABC = \frac{1}{2} \times (AB \times BC) \times \sin \theta$$

$$= \frac{1}{2} \times (10.3 \times 11.8) \times \sin 52.11$$

$$= (60.77) \times (\sin 52.11)$$

$$= 47.95 \text{ cm}^2$$

Soln 4 (d) - (i) Convert 98° to radians.

\Rightarrow As we know,

$$180^\circ \longrightarrow \pi \text{ radians.}$$

$$\therefore 98^\circ \longrightarrow x.$$

$$\therefore x = \frac{98}{180} \times \pi$$

$$[x = 0.54 \pi] \text{ radians.}$$

Soln. 4 (d) - (ii)

$$\text{Area of a sector} = \pi r^2 \times \frac{\theta}{360^\circ}$$

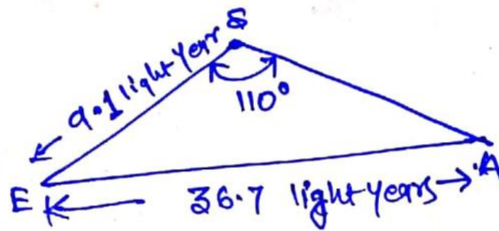
$$= \pi \times 2.8^2 \times \frac{98}{360}$$

$$(\because r = 2.8 \text{ cm})$$

$$= 6.704 \text{ cm}^2$$

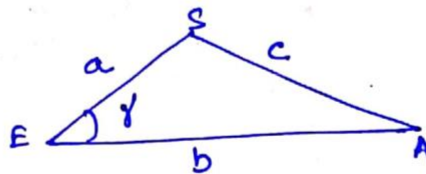
Solution (5) (a)

E → Earth
A → Arcturus.
S → current position.



Solution (5) - (b)

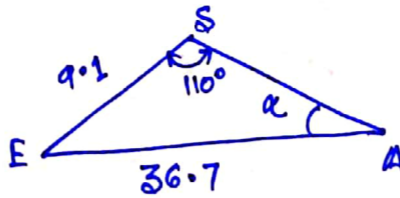
-As cosine rule states.



$$c = \sqrt{a^2 + b^2 - 2ab \cos \gamma}$$

she cannot directly put cosine rule as γ angle is unknown for ~~any~~ value of side (c)
calculating

Solution (5) - (c) / (i)



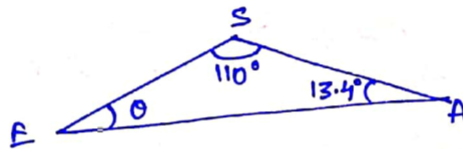
Apply sine law.

$$\frac{9.1}{\sin \alpha} = \frac{36.7}{\sin 110^\circ}$$

$$\begin{aligned} \sin \alpha &= \frac{9.1}{36.7} \times \sin 110^\circ \\ &= 0.247 \times (\sin 110^\circ) \\ &= 0.232 \end{aligned}$$

$$\begin{aligned} \alpha &= \sin^{-1}(0.232) \\ [\alpha &= 13.42^\circ] // \end{aligned}$$

Soln 5 - (c) / (ii)



As we know,

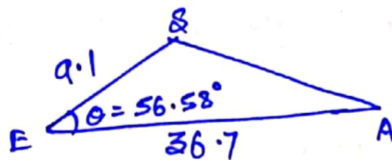
Sum of all angles in $\Delta = 180^\circ$

i.e.,

$$\theta + 110 + 13.42 = 180$$

$$\begin{aligned} \therefore \theta &= 180 - (110 + 13.42) \\ [\theta &= 56.58^\circ] \end{aligned}$$

Soln 5 (c) / (iii)



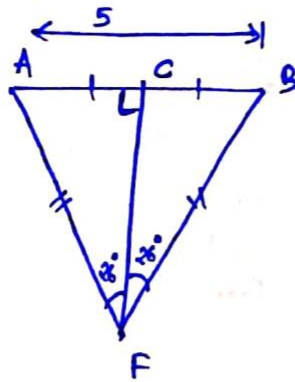
Apply cosine rule.

$$\begin{aligned} SA &= \sqrt{(SE)^2 + (EA)^2 - 2 \cdot (SE)(EA) \cos 56.58} \\ &= \sqrt{(9.1)^2 + (36.7)^2 - 2(9.1)(36.7) \cos(56.58)} \end{aligned}$$

$$SA = \underline{\underline{32.58 \text{ Hqmt (Approx)}}}$$

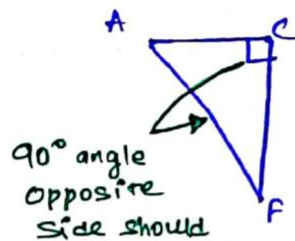
Years

Solution 6(a)



As per the property of right angle triangle.

Side opposite to the right angle triangle should be largest i.e., AF & BF



90° angle opposite side should

be greater (or more)

as compared to other two sides

$$\left\{ \begin{array}{l} AC = 2.5m \\ CF = 6.5m \end{array} \right.$$

↓
as calculated by student.

Solution 6(b)

There is a cross-multiplication error, as student performing division instead of multiplication for finding the side CF.

error 2 → ~~as~~ calculated value of side CF is "wrong".

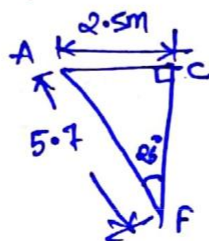
$$CF = \cos 26^\circ \times 5.7$$

$$[CF = 5.12m]$$

§

Solution 6(c) → "NO" → it can easily be found by putting the value of $\tan \theta$

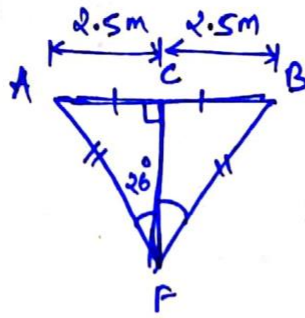
i.e.,



$$\tan \theta = \frac{AC}{CF}$$

$$\tan 26^\circ = \frac{2.5}{CF} \therefore CF = 5.12m$$

Solution 6(d)



By Congruency of a ~~right~~ triangle $\triangle ACF$ and $\triangle BCF$

$$AC = BC = 2.5m$$

$\therefore \angle ACF = \angle BCF$
 $\Rightarrow AF = BF$ (given)
CF = common
Hence using this \triangle 's congruence)

Now, in $\triangle ACF$

$$\tan \theta = \frac{AC}{CF}$$

$$\tan 26^\circ = \frac{2.5}{CF}$$

$$[CF = 5.12m]$$

Solution 7(a) \rightarrow "STATISTICS"

I ~~am~~ found statistics is relevant and interesting because of its usage to find out relevant detail from the given "RAW DATA"

Solution 7(b) \rightarrow "Yes" I feel confident ~~to~~ in chosen topic "STATISTICS"

I can take random data of any particular field and can make detailed research on it using "STATISTICAL TACTICS", like finding out Data frequency, Mean, MODE, MEDIAN etc.